Prediction of Essential Genes based on Machine Learning and Information Theoretic Features

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Abstract: Computational tools have enabled a relatively simple prediction of essential genes (EGs), which would otherwise be done by costly and tedious gene knockout experimental procedures. We present a machine learning based predictor using information-theoretic features derived exclusively from DNA sequences. We used entropy, mutual information, conditional mutual information, and Markov chain models as features. We employed a support vector machine (SVM) classifier and predicted the EGs in 15 prokaryotic genomes. A five-fold cross-validation on the bacteria *E. coli*, *B. subtilis*, and *M. pulmonis* resulted in AUC score of 0.85, 0.81, and 0.89, respectively. In cross-organism prediction, the EGs of a given bacterium are predicted using a model trained on the rest of the bacteria. AUC scores ranging from 0.66 to 0.9 and averaging 0.8 were obtained. The average AUC of the classifier on a one-to-one prediction among *E. coli*, *B. subtilis*, and *Acinetobacter* is 0.85. The performance of our predictor is comparable with recent and state-of-the-art predictors. Considering that we used only sequence information on a problem that is much more complicated, the achieved results are very good.

1 INTRODUCTION

The subset of genes which are absolutely necessary for the survival of an organism are called essential genes (EGs). Identification of these genes is very important for understanding the minimal requirements for maintaining life (Itaya, 1995). EGs can be used as potential drug targets for directed drug design against pathogens (Chalker and Lunsford, 2002; Lamichhane et al., 2003). In synthetic biology, studies on EGs are very crucial for re-engineering microorganisms and building a minimal genome (Hutchison et al., 2016).

Traditionally, experimental procedures such as single gene knockout experiments (Chen et al., 2015; Giaever et al., 2002), transposon mutagenesis (Salama et al., 2004), and RNA interference (Cullen and Arndt, 2005) are used to identify the EGs. Although the experimental methods are fairly accurate, they are often time-consuming, expensive, and laborious. Thus, various computational prediction methods have been proposed (Chen and Xu, 2005; Acencio and Lemke, 2009). The earliest computational methods were based on comparative genomics in which gene essentiality annotations are transferred among species through homology mappings (Mushegian and Koonin, 1996; Zhang et al., 2016). Later on, as the gene essentiality data of some model organisms became available in public databases (such as DEG (Luo et al., 2014), CEG (Ye et al., 2013), and OGEE (Chen et al., 2012)), researchers have extensively studied the characteristics and features of EGs and non-essential genes (NEGs) to deploy computational methods of prediction. The proposed methods make use of sequence information (e.g., protein length, strand bias, and amino acid composition) (Ning et al., 2014; Song et al., 2014), network topology (e.g., degree centrality and betweenness centrality) (Plaimas et al., 2010; Acencio and Lemke, 2009; Lu et al., 2014), gene expression (e.g., mRNA expression level and fluctuations in gene-expression) (Deng et al., 2011; Cheng et al., 2014), and functional domain (e.g., domain enrichment) based features (Deng et al., 2011). The features or their combinations are then utilized along with machine learning algorithms for predicting EGs.

Except for the sequence-based features, which can be obtained from the primary DNA or gene sequences, the others require some sort of precomputed experimental data. Network topology based features require the availability or construction of protein-protein interaction, gene regulatory networks, or metabolic networks. Similarly, the gene expression and functional domain features demand the expres-
sion data and a search in protein domain databases such as PROSITE and PFAM. Although experimental and genetic network information is available for the well-studied organisms, they are not available for all organisms, especially for newly sequenced and under-studied organisms. Hence, we intended to produce a machine learning based predictor relying only on primary sequence information. Ning et al. (Ning et al., 2014) proposed a gene essentiality predictor that uses only primary sequence information and showed that decent results can be obtained. They used nucleotide, di-nucleotide, codon, and amino acid frequencies along with what is known as CodonW features. The CodonW features, which are sequence derived, are obtained from a codon usage analysis software (http://codonw.sourceforge.net). However, some of the features in the CodonW features are not purely obtainable from the primary sequence. For instance, the Codon Adaptation Index (CAI) is a measure of the relative adaptability of the codon usage of a gene compared to the codon usage of highly expressed genes (Sharp and Li, 1987). That means, one needs to first distinguish the highly expressed genes in the organism. The other very effective essential gene predictor based solely on sequence and sequence derived properties is ZUPLS (Song et al., 2014). ZUPLS uses features from the so-called Z-curve, sequence based (e.g., size, CAI, and strand), homology mapping, and domain enrichment scores. Note that the latter two require database searches.

In this work, we present a machine-learning based essential gene predictor using information-theoretic features derived exclusively from the DNA sequences. The information-theoretic features are entropy (Shannon and Gibbs), mutual information (MI), conditional mutual information (CMI), and Markov parameters. These quantities measure the structural and organizational properties in the DNA sequences. The entropy computations will highlight the degree of randomness and thermodynamic stability of the genes. In a previous study (Nigatu et al., 2016), we have extensively analyzed the application and implication of Shannon and Gibbs entropies in bacterial genomes. MI has been extensively used in various computational biology and bioinformatics applications. For instance, MI profiles were used as a genomic signatures to reveal phylogenetic relationships between genomic sequences (Bauer et al., 2008), as a metric of phylogenetic profile similarity (Date and Marcotte, 2003), and for identification of single nucleotide polymorphisms (SNPs) (Hagenauer et al., 2004). Hence, MI and CMI features make use of sequence organization and dependencies and capture the differences between EGs and NEGs. The Markov features are selected for measuring statistical dependencies inside the genes. Assuming that the gene sequences of EGs and NEGs are generated by Markov sources of order $m$ and $n$, respectively. We first estimate the Markov orders from the genes in the training sets and construct the corresponding Markov chains. Then, the genes in the test dataset are scored using the two Markov chains. The scores are used as Markov features. After the features are collected, we employ a support vector machine (SVM) to perform a supervised classification.

To our knowledge, the only essential gene predictor which uses solely sequence composition information is the work of Ning et al. (Ning et al., 2014). Hence, we have tested our method on the organisms used in their work, to allow for easy performance comparisons.

2 METHODS

2.1 Data Sources

The dataset for essential and non-essential protein coding genes were obtained from the database of essential genes (DEG 13.5). DEG collects the list of essential and non-essential genes in both eukaryotes and prokaryotes, which were identified by different experimental procedures such as single gene knock-out and RNA interference (Luo et al., 2014). The list and accession number of the bacteria used in this study is presented in Table 1. The genome sequences and the corresponding annotations were downloaded from NCBI GenBank (Benson et al., 2013).

2.2 Information Theoretic Features

2.2.1 Mutual Information (MI)

The mutual information measures the information shared by two random variables $X$ and $Y$. It is the amount of information provided by one random variable about the other. We took $X$ and $Y$ to be two bases located $k$ bases apart. Mathematically, MI at a distance $k$ between $X$ and $Y$ with a joint probability $P_k(x, y)$ is given by

$$I_k(X,Y) = \sum_{x \in \Omega} \sum_{y \in \Omega} P_k(x,y) \log_2 \frac{P_k(x,y)}{P(x)P(y)},$$

where $P(x)$ and $P(y)$ are the marginal probabilities of $X$ and $Y$, respectively. $\Omega$ is the set of nucleotides $\{A,T,C,G\}$. For a given gene, the joint and marginal
<table>
<thead>
<tr>
<th>No.</th>
<th>Organism</th>
<th>Abbreviation</th>
<th>Accession No.</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>Acinetobacter baylyi ADP1</td>
<td>AB</td>
<td>NC_005966</td>
</tr>
<tr>
<td>2</td>
<td>Bacillus subtilis 168</td>
<td>BS</td>
<td>NC_000964</td>
</tr>
<tr>
<td>3</td>
<td>Escherichia coli MG1655</td>
<td>EC</td>
<td>NC_000913</td>
</tr>
<tr>
<td>4</td>
<td>Francisella novicida U112</td>
<td>FN</td>
<td>NC_008601</td>
</tr>
<tr>
<td>5</td>
<td>Haemophilus influenzae Rd KW20</td>
<td>HI</td>
<td>NC_009007</td>
</tr>
<tr>
<td>6</td>
<td>Helicobacter pylori 26695</td>
<td>HP</td>
<td>NC_00915</td>
</tr>
<tr>
<td>7</td>
<td>Mycoplasma genitalium G37</td>
<td>MG</td>
<td>NC_009008</td>
</tr>
<tr>
<td>8</td>
<td>Mycoplasma pulmonis UAB CTIP</td>
<td>MP</td>
<td>NC_002771</td>
</tr>
<tr>
<td>9</td>
<td>Mycobacterium tuberculosis H37Rv</td>
<td>MT</td>
<td>NC_00962</td>
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<td>10</td>
<td>Pseudomonas aeruginosa UCBPP-PA14</td>
<td>PA</td>
<td>NC_008463</td>
</tr>
<tr>
<td>11</td>
<td>Staphylococcus aureus N315</td>
<td>SA</td>
<td>NC_002745</td>
</tr>
<tr>
<td>12</td>
<td>Staphylococcus aureus NCTC 8325</td>
<td>SA2</td>
<td>NC_007795</td>
</tr>
<tr>
<td>13</td>
<td>Salmonella enterica serovar Typhi</td>
<td>SE</td>
<td>NC_004631</td>
</tr>
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<td>14</td>
<td>Salmonella typhimurium LT2</td>
<td>ST</td>
<td>NC_003197</td>
</tr>
<tr>
<td>15</td>
<td>Vibrio cholerae N16961</td>
<td>VC</td>
<td>NC_002505</td>
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<tr>
<td>16</td>
<td>Salmonella enterica serovar Typhimurium SL1344</td>
<td>SE2</td>
<td>NC_016810</td>
</tr>
</tbody>
</table>

Probabilities are estimated from the relative frequencies of the di-nucleotides and nucleotides, respectively. Bauer et al. (Bauer et al., 2008), used this definition (Eq. 1) and computed the profile of the average mutual information function to produce a genomic signature that can uniquely identify species.

The mutual information evaluation, using Eq. 1, will result in a single value. However, we have instead used the components of the definition, i.e., without the summations, as features (16 features). That means, for each di-nucleotide, the quantity \( P_z(x,y) \log_2 \frac{P(x,y)}{P(x)P(y)} \) is calculated and taken as a feature. We have tested the classifier for different distances (i.e., \( k = 1, 2, 3 \ldots \)) and the performance has decayed very fast with increasing distance. Thus, we have decided to use the MI between consecutive bases (\( k = 1 \)).

### 2.2.2 Conditional Mutual Information (CMI)

The mutual information between two random variables \( X \) and \( Y \) conditioned on a third random variable \( Z \) having a probability mass function (pmf) \( P(z) \) is given by

\[
I(X;Y|Z) = \sum_{z \in \Omega} P(z) \sum_{x \in \Omega} \sum_{y \in \Omega} P(x,y|z) \log_2 \frac{P(x,y|z)}{P(x|z)P(y|z)}
\]

\[
= \sum_{x \in \Omega} \sum_{y \in \Omega} \sum_{z \in \Omega} P(x,y,z) \log_2 \frac{P(x,y,z)}{P(x,z)P(y,z)}
\]  

where \( P(xyz), P(xz), \) and \( P(yz) \) are the joint pmfs of the random variables shown in brackets.

Similar to the MI function, the CMI can be defined as a function of the distance between two bases, which we regard as random variables \( X \) and \( Y \). For example, \( CMI(d) \) would mean the MI between two bases located \( d \) bases apart conditioned on the \( d \) bases in the middle. Note that, the CMI expression in Eq. 2 reduces to the MI in Eq. 1, if \( X \) and \( Y \) are consecutive (\( d = 0 \)).

Again, the components of the CMI expression in Eq. 2 (without the summations) will be taken as CMI features. For all possible values of \( XYZ \), the quantity \( P(x,y,z) \log_2 \frac{P(x,y,z)}{P(x,z)P(y,z)} \) will be calculated and taken as a feature. Thus, the number of features depends on the length of \( Z (4^d) \). Here also, we have investigated the performance of the classifier for increasing distance. The performance of the classifier decays very quickly as the distance increases. Hence, we use \( CMI(1) \) as a feature (64 features).

### 2.2.3 Entropy (E)

The Shannon entropy quantifies the average information content of the gene sequence from the distribution of symbols. It is mathematically given as

\[
H_N = - \sum_i P_i^{(N)}(i) \log_2 P_i^{(N)}(i)
\]  

where \( P_i^{(N)}(i) \) is the probability (relative frequency) to observe the \( i \)th word of block size \( N \). We calculated the Shannon entropy of the genes for a block size of 3 (i.e. codons).

In our previous works (Nigatu et al., 2016; Nigatu et al., 2014), we have measured the information content in DNA sequences along with the thermodynamic
stability. We measured stability using Gibbs entropy. The Gibbs entropy is defined as
\[ S_G = -k_B \sum_i P_G(i) \ln P_G(i), \] (4)
where \( P_G(i) \) is the probability that a molecule is in the \( i \)-th state. We associated the probability distribution with the thermodynamic stability quantified by the nearest-neighbor free energy parameters. We used SantaLucia’s unified free energy parameters for di-nucleotide steps at 37°C as in (SantaLucia, 1998). The probability distribution, \( P_G(i) \), is modeled by the Boltzmann distribution given by
\[ P_G(i) = \frac{n_i e^{-\frac{E(i)}{k_B T}}}{\sum_j n_{j} e^{-\frac{E(j)}{k_B T}}}. \] (5)

\( n_i \) is the frequency of the the \( i \)-th codon and \( E(i) \) is the energy of the codon according to (SantaLucia, 1998), and \( T \) is the temperature in Kelvin.

We have computed the Shannon and Gibbs entropies of the genes and used them as an entropy feature.

### 2.2.4 Markov (M)

First, the correct Markov chain order for both EGs and NEGs in the training dataset is estimated. Then, two Markov chains of the estimated orders are constructed. After that, the features are computed by scoring every gene using the generated Markov chains.

Numerous Markov chain order estimators have been put forth in the literature. We have assessed the performances of selected estimators (Tong, 1975; Katz, 1981; Peres and Shields, 2005; Dalevi and Dubhashi, 2005; Menéndez et al., 2011) on DNA sequence data and selected the estimator proposed by Papapetrou and Kugiumtzis (Papapetrou and Kugiumtzis, 2013). The order estimation is based on CMI given in Eq. 2. A Markov chain of order \( L \) has the following property.
\[ P(x_n|x_{n-1}, \ldots, x_{n-L}, x_{n-L-1}, \ldots) = P(x_n|x_{n-1}, \ldots, x_{n-L}). \] (6)

Hence, for any \( m \leq L \), two nucleotides will be dependent and the CMI (conditioned on the \( m-1 \) intermediate values) will be greater than zero. Conversely, for \( m > L \), the two nucleotides will be independent given the intermediate values and CMI will be zero. Using this observation, they have proposed both parametric and non-parametric significance testing procedures (Papapetrou and Kugiumtzis, 2013; Papapetrou and Kugiumtzis, 2016). The parametric approximation of the CMI by a gamma distribution is more accurate than the other approximations (Papapetrou and Kugiumtzis, 2016). In a symbol sequence of length \( N \), \( I(X;Y|Z) \), the estimate of the CMI, is approximated by the gamma distribution,
\[ I(X;Y|Z) \approx \frac{\ln 2}{N} \Gamma\left(\frac{|Z|}{2}\right) \frac{1}{(|Y| - 1) \ln 2}. \] (7)
The gamma distribution is used as the distribution of the null hypothesis, \( H_0 : \text{CMI}(m) > 0 \). Since \( \text{CMI} \geq 0 \) always holds, one-sided parameter testing is performed. Thus, the \( p \)-value is computed from the complementary cumulative distribution of the gamma distribution in Eq. 7. \( H_0 \) is rejected if the \( p \)-value is less than the nominal significance level (\( \alpha = 0.05 \)). When \( H_0 \) is rejected, the next order is checked and the process continues until the null hypothesis is accepted.

After the correct order is determined for the EGs and NEGs, separately, two Markov chains of the estimated orders will be constructed. Then, the constructed Markov chains are used to score genes in both the training and test data sets. If the gene sequence is \( b_1, b_2, b_3, \ldots, b_l \) and \( m \) is the order of the Markov chain, the score is calculated as
\[ \text{Score} = \sum_{i=1}^{L-m} P(b_i | b_{i+1} \ldots b_{i+m}) \log_2 \left( \frac{P(b_{i+m} | b_{i+1} \ldots b_{i+m-1})}{P(b_{i+m})} \right). \] (8)
The score gives an indication of how likely the gene sequence is generated by the Markov chain compared to a random generation. The probability of the nucleotides is estimated from the frequencies in the training set, whereas the conditional probabilities are the entries of the Markov chain. The scores of a gene sequence on the two Markov chains (EG and NEG) are used as two features.

### 2.3 Classifier Design, Training, and Evaluation

The analysis is performed using Python 3.5.2 with scikit-learn module (Pedregosa et al., 2011). We used the SVM classifier to train and classify the EGs and NEGs. Mostly, the number of EGs is significantly lower than that of NEGs. This imbalance between the positive and negative datasets will cause a problem for machine learning algorithms (Visa and Ralescu, 2005; Provost, 2000). To overcome this problem, the datasets are balanced by randomly under-sampling the NEGs to the size of the EGs. The number of selections needed to cover all the NEGs can be determined.
from what is known as the Clarke and Carbon formula (Clarke and Carbon, 1976), i.e.,

$$N = \frac{\log(1 - p)}{\log(1 - \frac{\#EG}{\#NEG})}$$

(9)

where $p$ is the probability that a given gene is represented in the samples, $\#EG$ and $\#NEG$ are the number of essential and non-essential genes, respectively. This formula is widely used to calculate the coverage statistics in genome sequencing.

In the cross-organism predictions, one or a set of organisms are used to train the SVM classifier, whereas in the prediction of EGs in a given organism (intra-organism), the datasets are divided into training and test sets. In the five-fold cross-validation, the data is divided into five equal parts. The model is then trained on four parts and tested on the remaining one.

The flowchart in Fig. 1 presents the procedures followed in our EG and NEG classifier. To avoid the scaling differences between features, all features were standardized to zero mean and unit variance (feature scaling) prior to the training and testing of the classifier.

Different kernel functions (linear, radial basis function (rbf), and polynomial) and hyper-parameters (C and gamma) are considered. The C parameter in the SVM classifier optimizes the trade-off between misclassification of the training set and margin maximization (Ben-Hur and Weston, 2010). If C is small, training errors will increase whereas a larger C value leads to a hard margin. The gamma parameter in the rbf kernel defines the influence of training examples on the decision boundary. A large gamma means a smaller variance and the decision boundary is influenced by data points closer to the margin. The optimal values of C, gamma, and the type of kernel are

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**Figure 1:** A flow diagram of the classification procedure.
obtained by a grid-search approach.

The Area Under the Curve (AUC) of the Receiver Operating characteristic Curve (ROC) is used to evaluate the performance of our classifier. The ROC plots the true positive (TP) rate versus false positive (FP) rate. It shows the trade-off between sensitivity ($Sn$) and specificity ($Sp$) for all possible thresholds. Other performance evaluation such as Positive Predictive Value ($PPV$) and Accuracy ($Ac$) are also calculated. However, these parameters depend on the selected threshold value. Therefore, we will mainly use the AUC score for analyzing the performance of the classifier. For a given threshold, the true positive (TP), false negative (FN), false positive (FP), and true negative (TN) predictions are determined and $Sn$, $Sp$, $Ac$, and $PPV$ are calculated as follows:

$$Sn = \frac{TP}{TP + FN},$$
$$Sp = \frac{TN}{TN + FP},$$
$$PPV = \frac{TP}{TP + FP},$$
$$Ac = \frac{TP + TN}{TP + FN + TN + FP}.$$  \hspace{1cm} (10)

3 RESULTS AND DISCUSSION

3.1 Prediction of Essential Genes in *E. coli*

The number of essential genes (EG) in *E. coli* (296) is significantly lower than the number of non-essential genes (4077). As mentioned in Section 2, a balanced dataset is created by selecting an equal number of NEGs. 61 random samplings were performed (which ensures that 99% of NEGs are covered).

The balanced datasets were then passed to our SVM classifier. A linear kernel with $C = 0.5$ was selected to be the best hyperparameter using an extensive grid search. The features MI, M, and E are used. To evaluate the models performance, a 5-fold cross-validation is performed and the ROC curve and AUC values for the individual features as well as their combinations are presented in Fig. 2.

The estimated order for both the positive (EG) and negative (NEG) samples was found to be five. Hence, a fifth order Markov chain is constructed from the training data sets and is used to score the genes. Collectively, an AUC score of 0.85 is obtained. The $Sn$, $Sp$, and $Ac$ of our classifier, with the probability threshold set at 0.5, are 0.88, 0.67, and 0.78, respectively. The entropy features, i.e., Shannon and Gibbs entropies produced the lowest performance. This could be because of the dependency between the Shannon and Gibbs entropies. Both of them make use of the codon frequencies. The Markov and MI features, even when used alone, produced a very good performance.

3.2 Prediction of Essential Genes in *M. pulmonis*

The same procedure is taken to train and predict the essential genes in *M. pulmonis*. A 5-fold cross-validation of the linear SVM classifier is performed on the balanced dataset. The 310 non-essential genes were selected out of 322 to balance the datasets. 20 random samplings were performed and the average
ROC curves and AUC values for all the learning attributes, individually and collectively, are presented in Fig. 3. The predicted order of the Markov chain, for both EGs and NEGs, was 6. Here also, the entropy features have produced the smallest values. The average AUC of the classifier using all the features is 0.81. The $Sn$, $Sp$, and $Ac$, at a threshold of 0.5, are 0.88, 0.62, and 0.75, respectively.

3.3 Prediction of Essential Genes in $B.\ subtilis$

According to DEG, $B.\ subtilis$ has 271 essential and 3904 non-essential genes. A similar undersampling of the non-essential genes is carried out and 65 random samplings were done. The ROC curves of the five-fold cross-validation are presented in Fig. 4. Interestingly, the estimated order from essential genes training set is 5 whereas for non-essential ones, the order is 4. Therefore, each gene is scored by an order 4 Markov chain constructed from the NEG training set and an order 5 Markov chain obtained from the EG training set.

The average AUC of the classifier using all the features is 0.89. The $Sn$, $Sp$, and $Ac$, at a threshold of 0.5, are 0.83, 0.75, and 0.8, respectively.

To check if the estimated Markov order is indeed better than the other orders, we have used features from the scores of fixed Markov orders ranging from 1 to 7 and tested the performance of our classifier. A linear SVM ($C = 0.5$) is applied on a balanced dataset using a single sample. The AUC scores for the prediction of essential genes in $B.\ subtilis$, $E.\ coli$, and $M.\ pulmonis$ are shown in Fig. 5. In $E.\ coli$, the estimated order is 5 and the maximum AUC score was obtained by using orders 4 and 5 (AUC = 0.84). In $B.\ subtilis$, the estimated order is order 4 for non-essential genes and order 5 for essential genes. The maximum AUC score of 0.83 is observed for order 6. However, the performance using the estimated orders is also 0.83. This is a good example to show how the order estimation finds the optimal performance, rather than a random choice of an order. $M.\ pulmonis$ has an estimated order of 6 and it is with order 6 Markov chain the maximum AUC is obtained (0.81). Therefore, this shows that the estimated order achieves the best possible AUC score.

3.4 Cross-organism Predictions

3.4.1 Many to One Predictions

So far, the training and test datasets have been taken from the same organism. However, a more interesting and useful approach would be to predict essential genes across, both closely and distantly related, organisms. This will enable the prediction of essential genes in newly sequenced organisms without having to do the tedious and time-consuming gene-knockout experiments. To make a cross-organism prediction, we have collected the essential and non-essential gene data of 15 bacterial species from DEG. We have used the same bacteria as in the study by Ning et al. for comparison purposes. We have left out the bacteria Streptococcus pneumoniae, since the NEG are not reported in the DEG database. There are a total of 6078 EGs and 33475 NEGs in the pool. A five-fold cross-validation was used to evaluate the performance of the SVM classifier. 6078 NEGs are randomly selected to
balance the datasets and the average AUC score of 10 random samplings was 0.79 using a linear SVM with the hyperparameter C set at 0.5. However, a cross-validation on the 6078 EGs is not practical in evaluating the performance of the classifier as we would be interested in figuring out the EGs and NEGs of a new organism, which is not in our pool of organisms. Hence, we should assess the performance of the SVM classifier by using a one against the rest strategy. That is, one bacterium is reserved for testing whereas the other 14 bacteria are used to train the model. Here also, under-sampling of the NEGs is performed to produce a balanced data set.

All of the information theoretic features, i.e., MI, CMI, E, and M, are used. However, since there are a total of more than 39,000 genes, the estimation of the Markov order will be computational demanding. In addition, since the training set will be a collection of genes from multiple organisms, performing order estimation does not make sense. Therefore, we decided to use two fixed order Markov chains, orders 2 and 5, to capture both short and long dependencies. After examining the possible kernel functions (linear, rbf, and polynomial) and hyperparameters using a random grid-search, the rbf kernel with the default parameters has produced the best performance. The results are presented in Table 2. The $Sn$, $Sp$, $Ac$, and $PPV$ values are decision threshold dependent and the reported values are with a threshold of 0.5.

The AUC scores of the cross-organism prediction were between 0.66 and 0.9. The average AUC score was 0.8, which is a very good result considering the fact that only primary sequence information was used for the prediction of essentiality. The lowest performance was the prediction of the mycoplasma genitalium (MG) essential genes. This could be due to the small number of genes (only 98 NEGs) the bacterium has and this will make it difficult for the SVM to yield correct classifications. It could also be associated with the quality of the data. EGs which are identified by transposon mutagenesis often contain systematic biases (Deng et al., 2011; Jacobs et al., 2003). Transposon mutagenesis involves random transposon insertions and the transposons mostly miss shorter proteins leading to a bias towards labeling shorter proteins as EGs. Furthermore, the prediction performances are highly dependent on the evolutionary distance between the bacteria used for training and testing. Fig. 6 shows the phylogenetic tree of the bacteria used in this study, constructed using the freely available Interactive Tree Of Life (iTOL) v3 tool (Letunic and Bork, 2016).

### 3.4.2 One-to-one Cross-organism Prediction

To further show the transferability of essential gene annotations across closely and distantly related species, we have selected two Gram-negative bacteria (EC and AB) and the Gram-positive BS. Then, we have done a one-to-one cross-organism prediction among the three bacteria. The features used are Markov chains of order 2 and 5, MI, CMI, and E.
The hyperparameters leading to a high performance are 0.4 for C and 0.005 for gamma (obtained by performing a grid-search on the parameters). The AUC scores of the cross-organism predictions are presented in Table 3.

Despite having different lifestyles and very large evolutionary distance (EC and BS diverged about a billion years ago), it is remarkable that essential and non-essential genes can be reciprocally transferred with a fairly high accuracy using only primary sequence information.

### 3.5 Comparison with Other EG Predictors

Our EG predictor uses information theoretic features derived from primary sequence information only. The essentiality of a gene however is a complex issue, which not only depends on sequence composition and organization but also on many other factors such as metabolic relationships between proteins, evolutionary conservation, and gene expression. The essentiality of a gene is also context dependent. A gene, which is essential in one condition, might not be essential in another conditions (Sassetti et al., 2001).

Hence, many researchers have tried to use gene expression, homology, and network topological information along with sequence-based features for the prediction of essential genes using various machine-learning algorithms. The work of Ning et al. (Ning et al., 2014), being the only purely primary sequence information based predictor, can be directly compared with our predictor. Although the other methods use extra information, which is sometimes hard to get for under-studied or newly discovered organisms, we have also made a comparison of our results with selected essential gene predictors.

Our results are overall slightly better than Ning et al. (Ning et al., 2014). For E. coli, the five-fold cross validation AUC score was 0.82, our method produced an AUC score of 0.85. The AUC for the prediction of M. pulmonis EGs is improved from 0.74 to 0.81. The cross-validation results of the 16 bacterial species had a 0.76 AUC score. Our method has also shown a comparable performance of 0.79. Tested on an independent test set using a strain of Salmonella Typhimurium SL1344, their model resulted in AUC score of 0.81. An independent test on all of the bacteria has produced AUC scores of up to 0.9 (on average 0.8). For the same Salmonella strain the AUC scores is 0.8.

Deng et al. (Deng et al., 2011) have used thirteen features. Along with the sequence dependent features such as length of amino acids and effective number of codons, they have used features related to network topology, gene-expression, homology, phylogenetics, and protein domain knowledge. A combination of four machine-learning algorithms (Nave Bayes, logistic regression, C4.5 decision tree, and CN2 rule) were applied. The other recent and more effective method for EG prediction is ZUPLS (Song et al., 2014). It uses Z-curve features together with other sequence-based features including homology (orthology and paralogy) and domain knowledge. They have adopted the partial least squares classifier for classification. The cross-organism prediction performances among the bacteria EC, BS, and AB are presented in the Table 4. In comparison, our method has a comparable performance with the two methods. The average values indicate that the ZUPLS method is slightly better in AUC score. However, our method has the highest performance in terms of PPV scores. Considering that we have used only primary sequence information, the performance of our classifier is astonishing.

### 4 CONCLUSIONS

We designed a machine learning based gene essentiality predictor and demonstrated the effective classification of essential and non-essential genes using
Table 3: AUC scores of essential gene prediction among AB, BS, and EC.

<table>
<thead>
<tr>
<th>Train</th>
<th>Test</th>
<th>AUC</th>
<th>Train</th>
<th>Test</th>
<th>AUC</th>
</tr>
</thead>
<tbody>
<tr>
<td>AB</td>
<td>BS</td>
<td>0.86</td>
<td>BS</td>
<td>EC</td>
<td>0.84</td>
</tr>
<tr>
<td>AB</td>
<td>EC</td>
<td>0.86</td>
<td>EC</td>
<td>AB</td>
<td>0.84</td>
</tr>
<tr>
<td>BS</td>
<td>AB</td>
<td>0.83</td>
<td>EC</td>
<td>BS</td>
<td>0.86</td>
</tr>
</tbody>
</table>

Table 4: Prediction performance comparison of our method, Deng et al. (Deng et al., 2011), and ZUPLS (Song et al., 2014).

<table>
<thead>
<tr>
<th></th>
<th>Our method</th>
<th>Deng et al.</th>
<th>ZUPLS</th>
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</thead>
<tbody>
<tr>
<td></td>
<td>Train</td>
<td>Test</td>
<td>AUC</td>
</tr>
<tr>
<td>EC</td>
<td>AB</td>
<td></td>
<td>0.84</td>
</tr>
<tr>
<td>EC</td>
<td>BS</td>
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<td>0.86</td>
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<td>AB</td>
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<tr>
<td><strong>Average</strong></td>
<td></td>
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<td><strong>0.85</strong></td>
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</tbody>
</table>

information-theoretic features. The features are directly derived from only the DNA sequence. Other computational methods depend on the availability of experimental data, such as network of gene/protein interactions, functional microarray gene expression, and gene ontology annotations. However, these experimental data are mostly only available for well-studied organisms and not for unstudied or newly sequenced organisms. In this regard, our method has an advantage that it can be applied to any organism. The information-theoretic tools we used are entropy, mutual information, conditional mutual information, and Markov models. These procedures are applied to the genomic sequences to reveal structural and compositional properties that can highlight differences between essential and non-essential genes. Average AUC scores of more than 0.8 were obtained. The AUC score for predicting EGs of *E. coli*, *B. subtilis*, and *M. pulmonis* are 0.85, 0.81, and 0.89, respectively. In cross-organism prediction, two approaches where taken. The first is a many-to-one approach where the EGs of a given bacteria are predicted using a model trained on multiple bacteria. The average AUC score is 0.8. The other is a one-to-one prediction between *E. coli*, *Acinetobacter*, and *B. subtilis* and average AUC of 0.85 was obtained. The performance of our predictor has been comparable to recent and state-of-the-art predictors. Considering that we used only sequence information on a problem that is much more complicated (essentiality is context dependent and involves the interaction of multiple proteins), the achieved results are very encouraging. In this work, we have tested our method on prokaryotic genomes and shown that EG annotations can be reciprocally transferred between both closely and distantly related bacteria with a reasonable accuracy. In the future, we will assess the applicability of our method in other domains of life. To further improve the accuracy in the many-to-one predictions, instead of using all species in the pool for training, a subset could be selected based on certain criteria (e.g., sequence similarity).

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**REFERENCES**


